

- Midterm Review + What to expect
  - Resolving grammatical ambiguities
    - Shift / reduce parsing
    - Longest match principle
  - Algorithms
    - Dynamic programming for regular expressions  
 $O(n^3 k)$
    - D.P for context free grammars (CYK)
    - $O(n)$  parsing of regular expressions  
(Finite automata)
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# ① Midterm Review

- Everything in Ocaml is an expression / term

- A few forms:

- Literals: 3, "abc", true, [2; 8], ...

- Variables

- Function applications

$f\ a$

"values"

- Function abstractions

$\text{fun } x \rightarrow$

Not  
"values"

- Let expressions

$\text{let } x =$

$\text{in}$

- Conditionals: if

then

else

Parenttheses only for

(a) Resolving precedence

## (a) Resolving precedence

" f e x "  $\rightarrow$  Do you mean

f (e x)  
or (f e) x ?  
Traditional  
meaning

## (b) Multi argument ADT constructors

Some 3 : int option

Node (3, Leaf, Leaf)

Constructor  $\uparrow$   $\uparrow$

Parentheses necessary for  
multi-argument constructors

`List.map (fun x -> x + 1) [1; 2; 3]` : Implicitly

List.map : ('a  $\rightarrow$  'b)  $\rightarrow$  ('a list  $\rightarrow$  'b list)

List.map : ('a → 'b) → ('a list → 'b list)

Implicitly

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## Evaluation rules

Transform expressions to other expressions,  
(sometimes)

$((+) 3 4) \rightarrow 7$

$(3)$   
↑

$((+) ((+) 3 4) ((+) 2 6))$

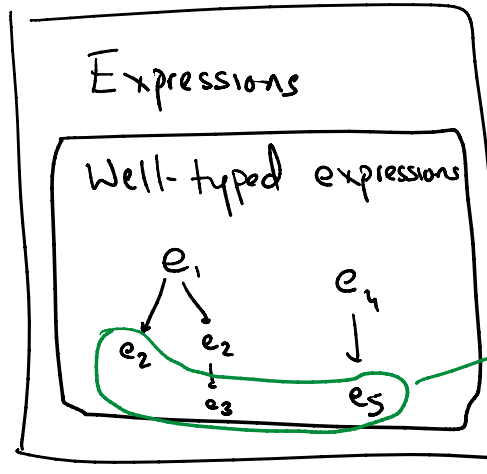
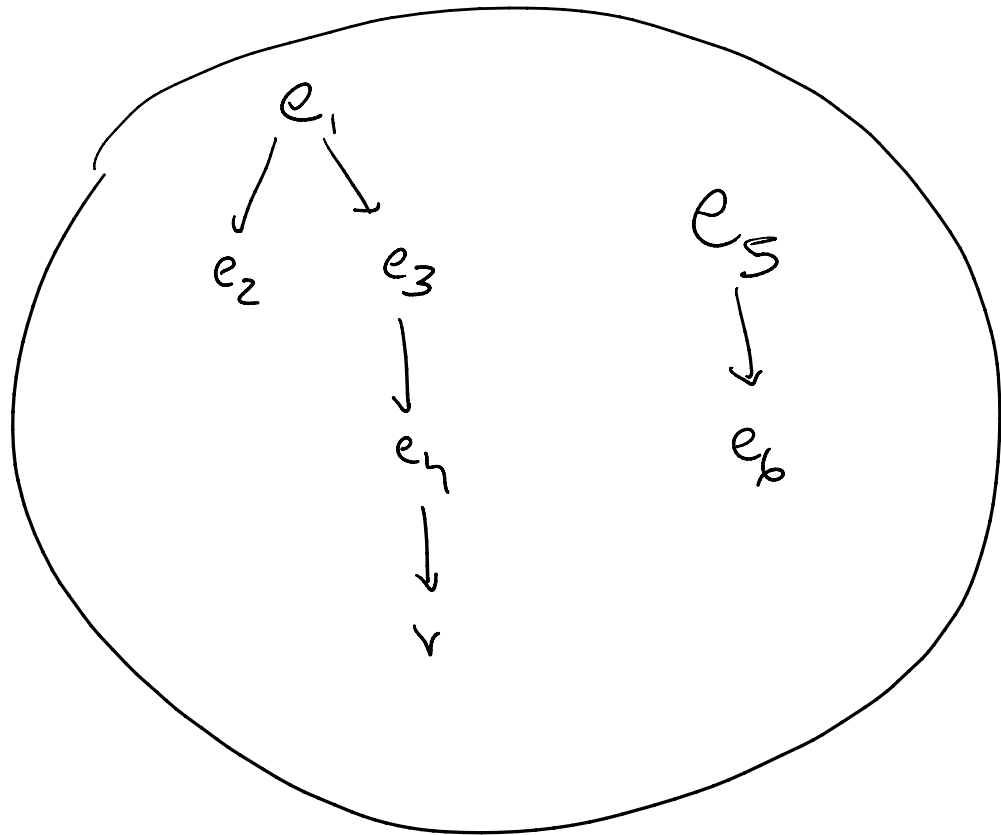
$((+) 7 ((+) 2 6))$

$((+) ((+) 3 4) 8)$

$((+) \rightarrow ((+) 2 c))$

$((+) ((+) 5 4) 8)$

# hiant forest of expressions



"Values"  
Expressions  
from which no

② Each value has  
a type

① more stepping  
can occur

③ Guarantee: If an expression is well-typed:  
then it either

(a) steps to another expression of the  
same type, or

(b) is a value

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## Midterm Questions 1—5

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① State type of some expression

② State expressions with some type

③ Show evaluation sequence

} predict result

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④ Scoping rules

⑤ Fix ...

⑤ Fix mistakes in ill-typed expression

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Midterm Questions (6), (7) Design

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⑥ Write program that solves problem  
(Algorithmic)

⑦ Design types for some application

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⑧ — ⑩: Random topics

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⑧ Tail recursion

⑨ Mutable references

⑩ List map & List fold

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# Resolving Grammatical Ambiguities

## Our almost-final calculator

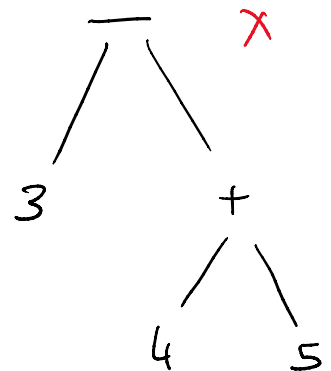
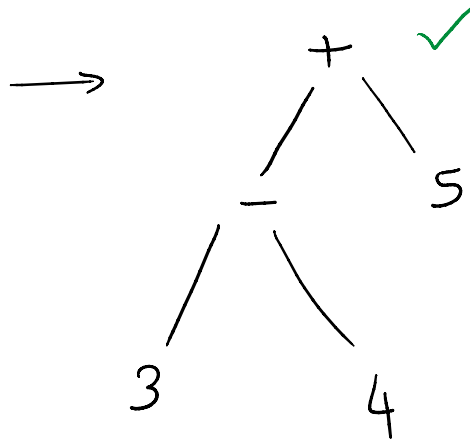
`(( "3 - 4 + 5" |> Lexing.from_string ) |> (top_expr read) ) |> eval`

`"3 - 4 + 5" |> Lexing.from_string |> ((top_expr read) |> eval)`

`"3 - 4 + 5" |> Lexing.from_string |> (top_expr read) |> eval`

Parser                      Lexical analyzer                      Evaluator

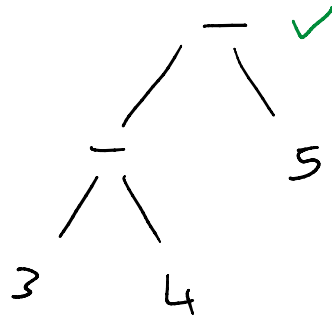
"3 - 4 + 5"



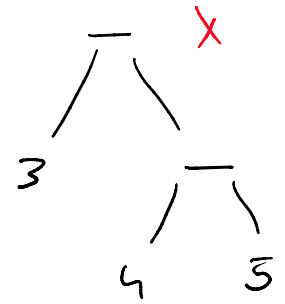


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"3-4-5"



Right sides of - & +  
are always integers



Left sides of -  
& + are  
integers