

Introduction to Types

Q1: How do we "construct" data?

Q2: How do we "deconstruct" data?



Nothing to do with
"destructors" / "finalizers".

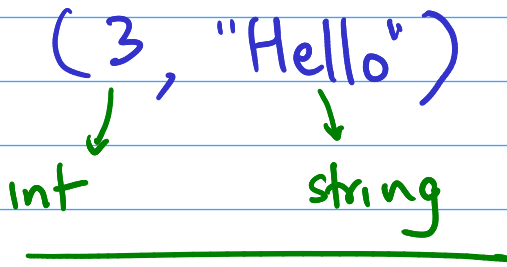
Foo() / ~Foo()

- Pairs, tuples, variants, records, lists

- Pattern matching

- ADT (algebraic data type) & recursion

Pairs



int * string

int - cross - string

fst : 'a * 'b → 'a
snd : 'a * 'b → 'b } "Accessors"

(3, "Hello") : constructor

Q : How to access the elements of a pair?

Only way for the pattern match to be successful is if p is a pair

let myfst (p) = let (p₁, p₂) = p in

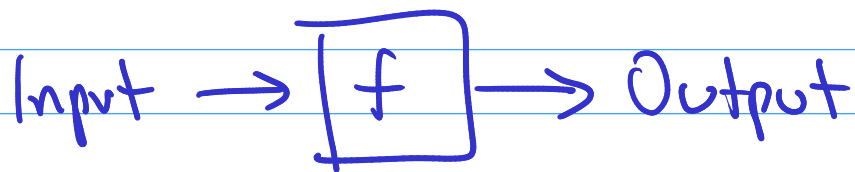
p₁

Deconstructor / Pattern match

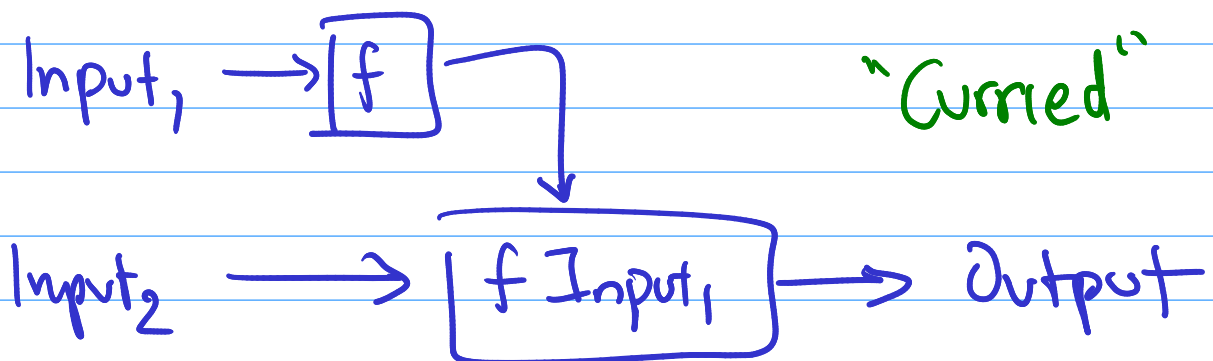
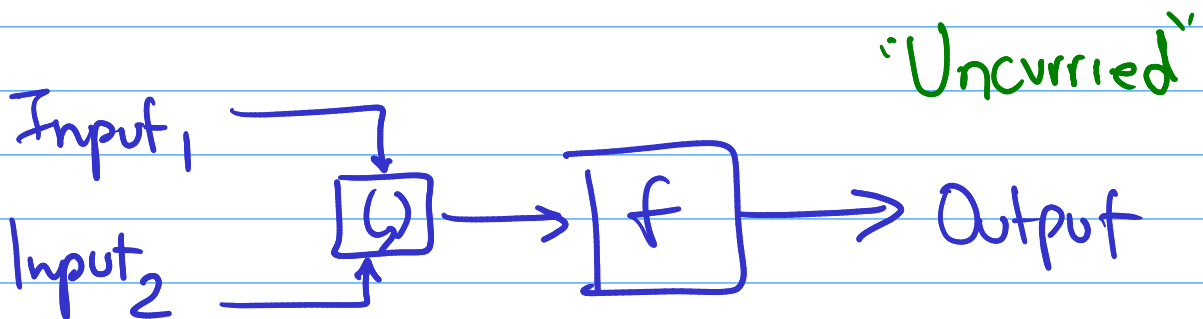
Bind p₁ to the first element of the pair

Bind p₂ to the second element.

Technically, every fn in Ocaml takes a single input & produces a single thing as output.



Q: How to derive functions with multiple inputs?



Lists

$[3; 4; 5] \rightarrow$ Syntactic sugar

Constructors $\left[\begin{array}{l} [] \rightarrow \text{Empty list} \\ a :: l \rightarrow \text{Take the list } l \text{ \& stick } a \text{ in front of it} \end{array} \right.$

$$[3; 4; 5] = 3 :: (4 :: (5 :: []))$$

Q: Check if a list is empty?

let is-empty $l = (\text{List.length } l) = 0$

- ① Who defines `List.length`?
- ② Requires $O(n)$ time

let is-empty l =

match l with

| [] → true

| hd::tl → false

let car l =

match l with

| [] → 0

| hd::tl → hd

car (3::(4::[]))

↙

3

Records

```
type person = { name: string; dob: int }
```

```
let p = { name = "Mukund"; dob = 1988 }
```

↓
Constructor

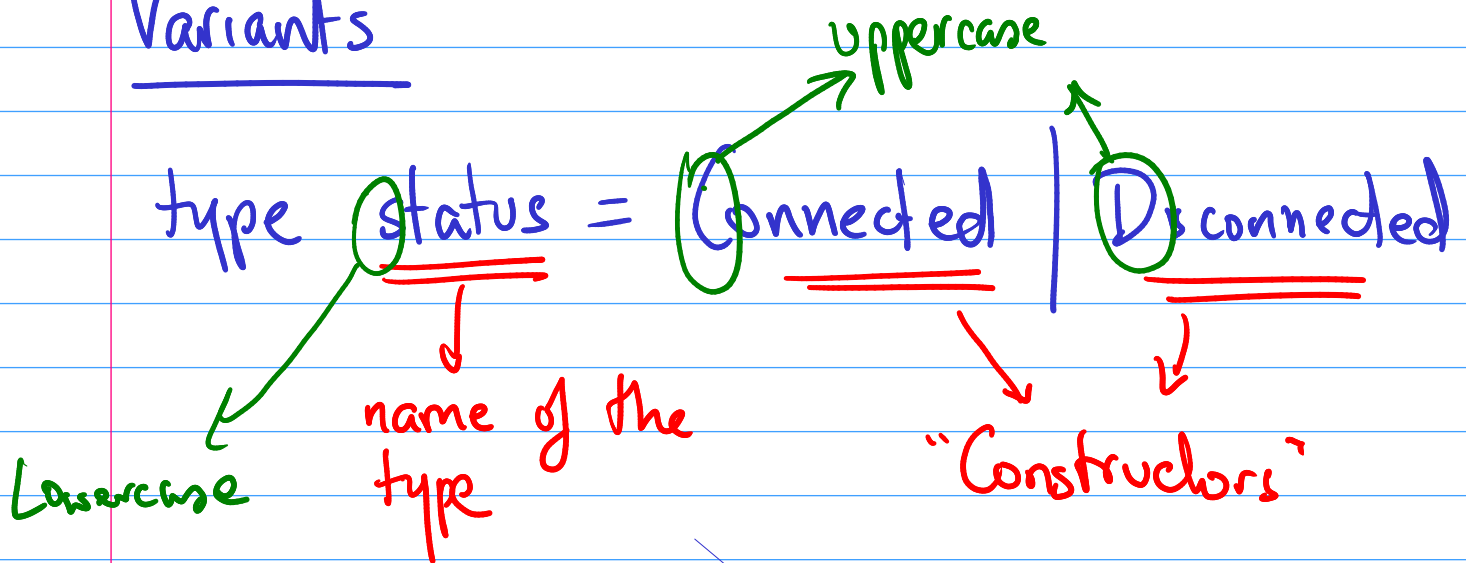
p.name p.dob
 ↘ ↙
 Accessors

```
let { name = pname; dob = pdob } = p
```

in pname ↘
 Deconstructor

Also, algebraic data type.

Variants

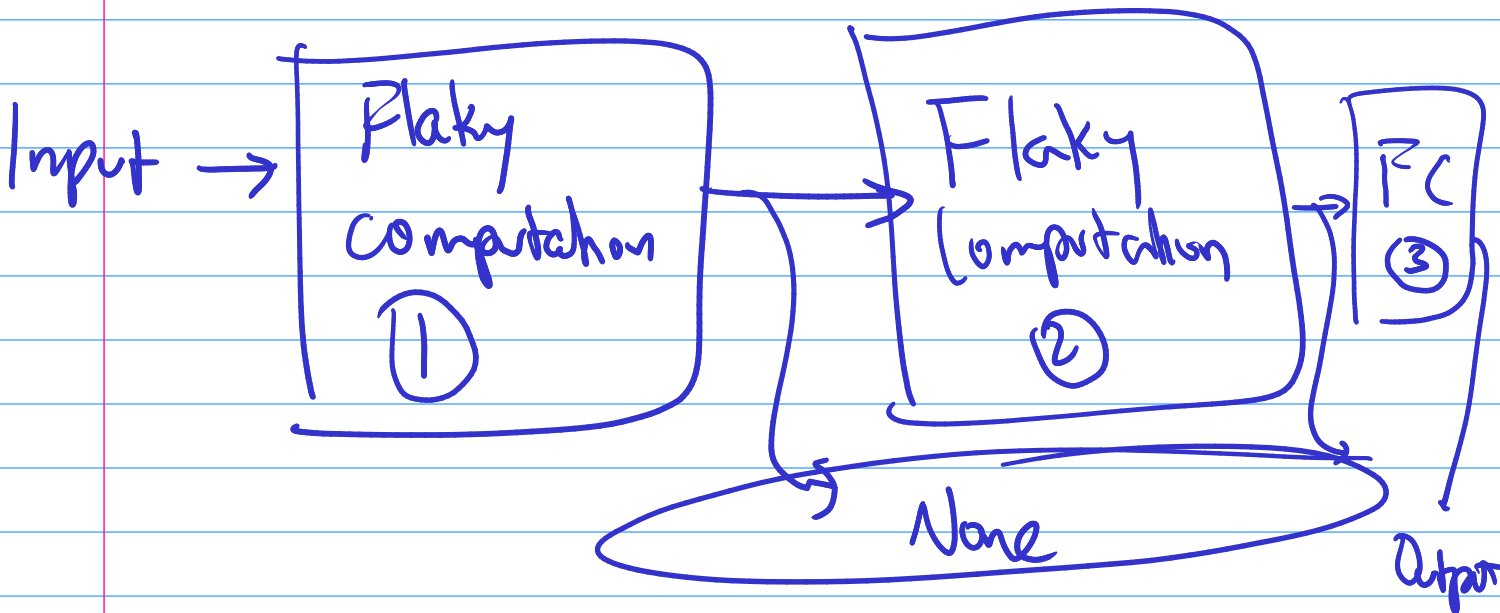
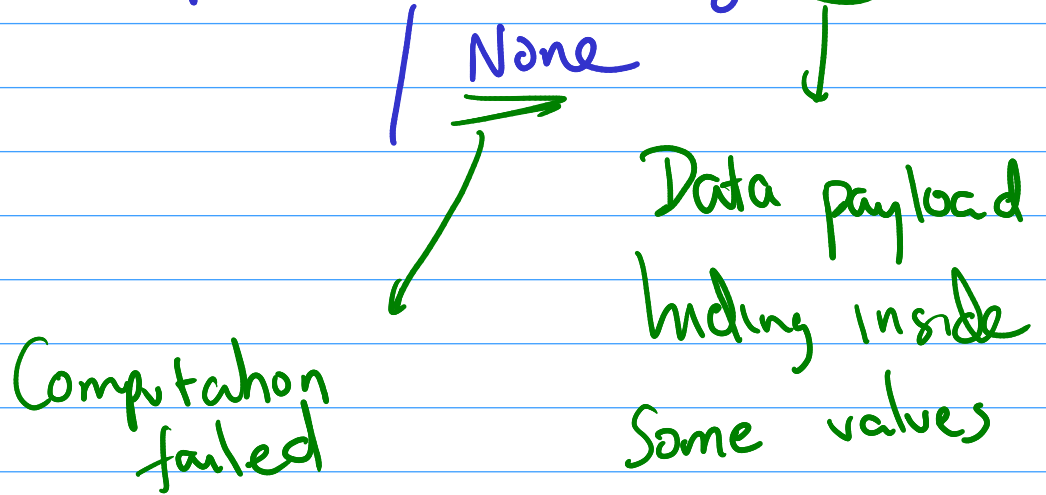


Claim 1: Connected \neq Disconnected

Claim 2: Every value of type status
is either Connected or Disconnected.

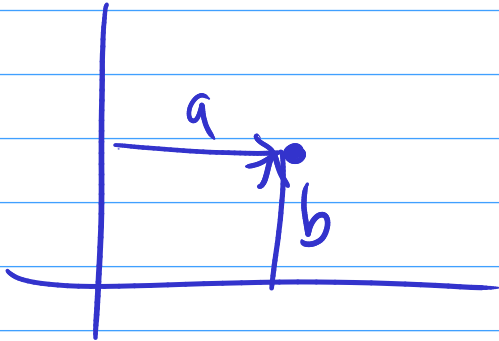
Option types

type 'a option = Some of 'a

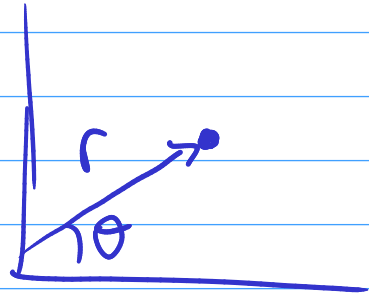


Maybe monad

Complex Numbers



Cartesian



Polar

type complex = Cartesian of int * int * int ↑ There are 16×10^{18} integers in our world.
| Polar of int * int

There are 16×10^{36} Cartesian

complex numbers.

There are 16×10^{36} Polar C.#s

In total, 32×10^{36} C.#s.