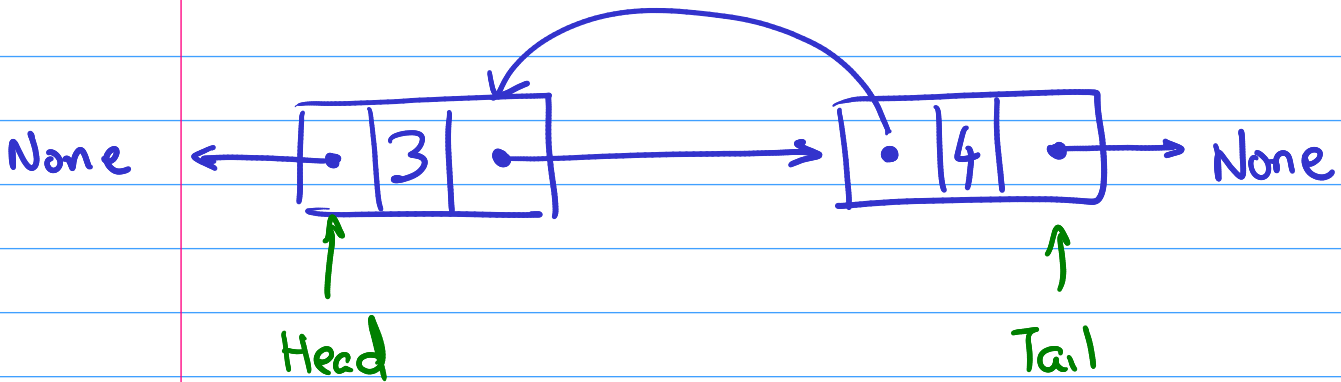


- Mutable Data Structures



- Defining recursive functions without rec!

```
let rec isEven n = if n = 0 then true else not (isEven (n - 1))
```

```
let isEven n =  
  let ans = ref true in  
  for i = 1 to n do  
    ans := not !ans  
  done;  
  !ans
```

```
let helper = ref (fun x -> true)
```

```
let isEven2 n = if n = 0 then true else not (!helper (n - 1))
```

```
helper := isEven2
```

↓
Ties the knot!

Now isEven2 works
correctly everywhere!

This function
returns the correct value
only sometimes!
- At $n=0$, intentionally
- At n odd, incidentally

Cycles in space cause cycles in time.

Equality

Structural equality	Physical equality	Something else?
'a → 'a → bool (=) (< >)	'a → 'a → bool (==) (!=)	
Checks if the two values have the same "shape"	Checks if values point to the same memory	

Rational Numbers

$$\frac{3}{5} \quad \frac{1}{2} \quad \frac{2}{4}$$

← Numerator
↑ Denominator

Intentional equality

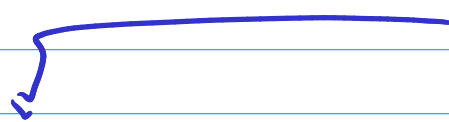
Checks if underlying object is the same thing.

Extensional equality

Checks if representations are equal



Structural equality



- ① For basic data types, check directly
- ② For ADTs, confirm that top-level ctor is the same; recursively check parameters

Function equality : "Undecidable" in general

No algorithm exists!

Structural equality of functions is undefined

Programming in the 'Large'

Q: How do we organize code?

Splitting into files / physical organizations

Functions, classes, Packages

Sense 1: Physical, syntactic organization

split code into files, directories

"Compilation units"

#include, #use, ...

Sense 2: Organizing names

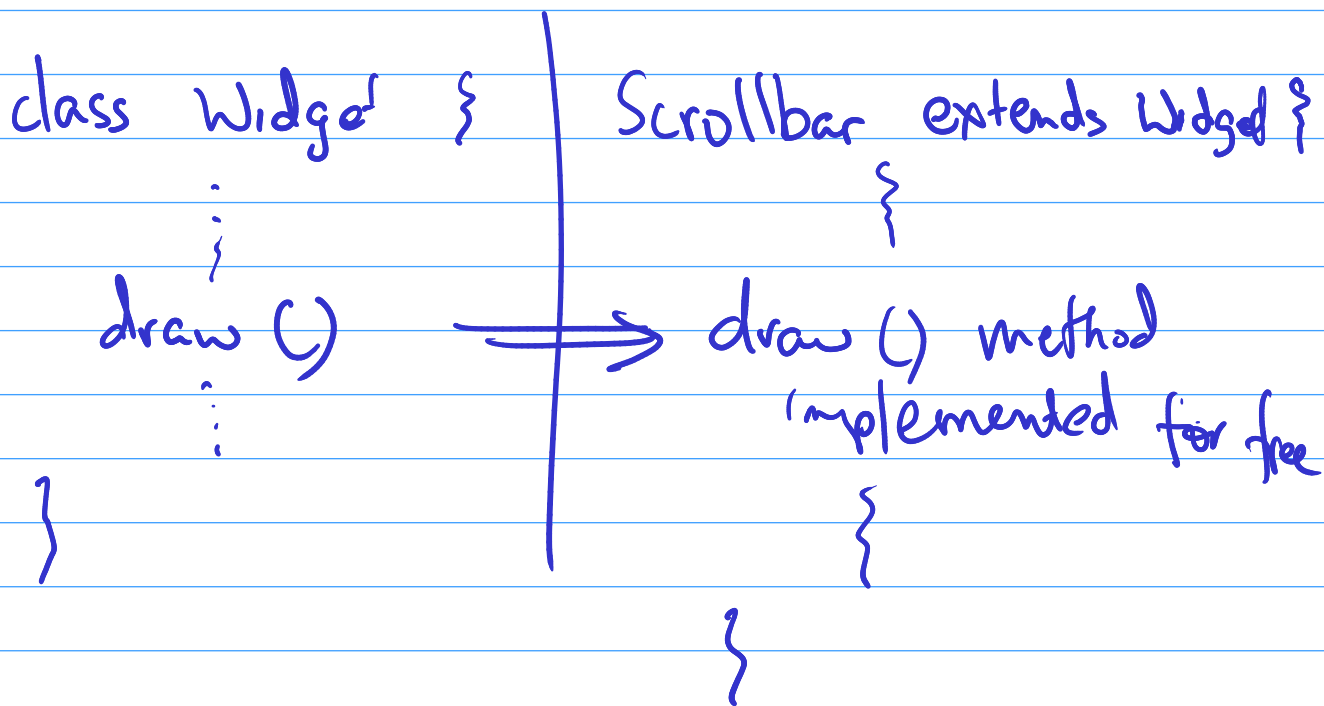
C++: namespaces scopes

Java: packages

Sense 3: Abstraction: Components interact through well-defined boundaries

Classes, Interfaces, Traits

Sense 4: Reuse of code



Inheritance ("ad-hoc polymorphism")

Parametric polymorphism

(OCaml, templates in C++,
generics in Java/C#/...)

OCaml : Module System

Two sublanguages

- ① Vernacular (expressions, values, types, fns, ...)
 - ② Module language
 - structure → implementation
 - signature → interface
- functor
-

C : Core / Preprocessor

C++ : Core / Templates / Preprocessor

Lisp : Core / Macros