

let rec sum n = if n = 0 then 0 else n + sum (n - 1)

$$\text{sum } 5 \Rightarrow \underline{\underline{5}} + \text{sum } (5-1)$$

$$\Rightarrow 5 + \text{sum } 4$$

$$\Rightarrow 5 + (4 + \text{sum } (4-1))$$

Work getting done

$$\Rightarrow 5 + (4 + \text{sum } 3)$$

$$\Rightarrow 5 + (4 + (3 + \text{sum } (3-1)))$$

$$\Rightarrow \dots$$

$$\Rightarrow 5 + (4 + (3 + (2 + (1 + 0))))$$

$$\Rightarrow 15$$

Work to be done

let rec helper acc n = if n = 0 then acc else helper (n + acc) (n - 1)

helper 0 5 \Rightarrow helper (5+0) (5-1)

\Rightarrow helper 5 4

\Rightarrow helper (4+5) (4-1)

\Rightarrow helper 9 3

$\Rightarrow \dots \Rightarrow$ helper 12 2

$\Rightarrow \dots \Rightarrow$ helper 14 1

$\Rightarrow \dots \Rightarrow$ helper 15 0

```
let rec sum n = if n = 0 then 0 else n + sum (n - 1)
```

Work that needs to be done "after the call"

```
let goodSum n =  
  let rec helper acc n = if n = 0 then acc else helper (n + acc) (n - 1) in  
  helper 0 n
```

No work needs to be done after the call.

```
let rec badRev l =  
  match l with  
  | [] -> []  
  | hd :: tl -> (badRev tl) @ [hd]
```

"Continuation" \Rightarrow Work to be done afterwards.

TAIL CALL RECURSION

```
let goodRev l =  
  let rec helper acc l =  
    match l with  
    | [] -> acc  
    | hd :: tl -> helper (hd :: acc) tl in  
  helper [] l
```

Empty continuation!
Nothing to be done afterwards!