

Lecture 26

- Announcements

- My grading deadline: May 18

May 14

- What remains still: - HW3 + HW4 ← May 10?

- Problem background + challenges ← - Project presentation

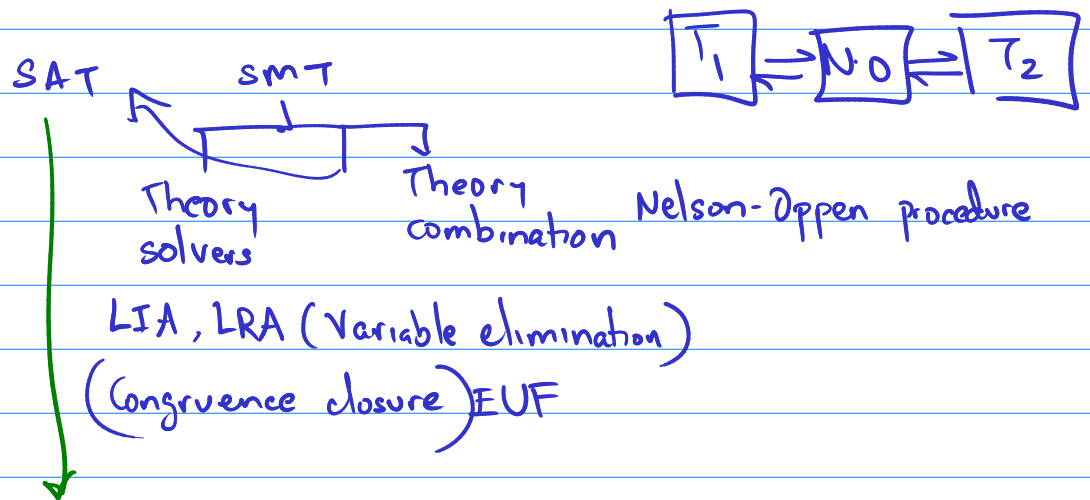
- What did you do? + Demo? - Project report (+ github links) ← May 14

- How well did it work? / Experiments

- What did you learn? What worked, what didn't work, why, etc.

① What did we discuss?

Unit 1: Constraint solvers



① What if the formula was unsatisfiable?
 - Convince me that it is unsat / why was it unsat?
 Unsat cores.

Automatic
 ④ Theorem provers
 for first order
 logic.

- How close is it to being satisfiable?
 Max SAT \longrightarrow Max SMT
 Weighted Max SAT

Vampire
 see TPTP Problems
 Thousands of Theorem Provers

② Ok, it is satisfiable. But how many satisfying assignments does it admit?

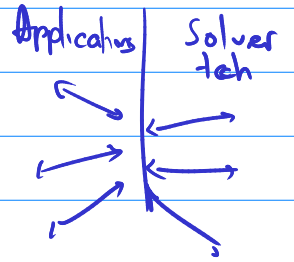
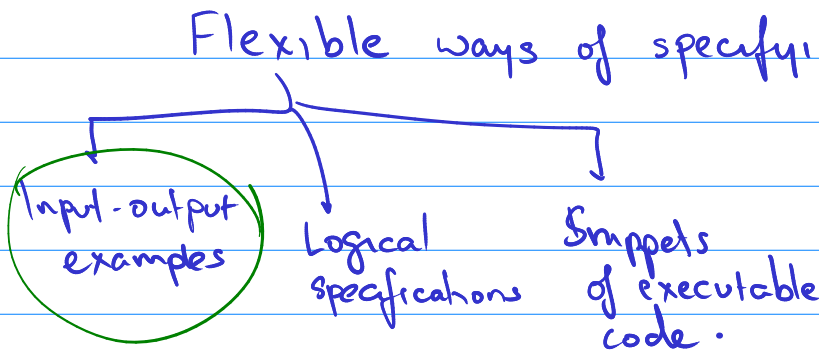
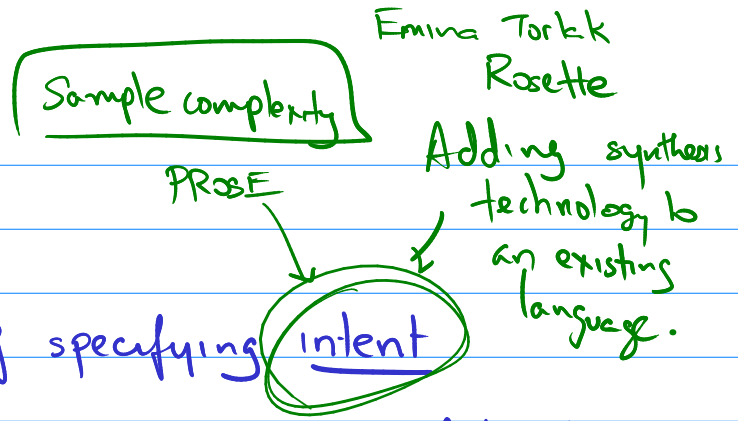
$P \vee (P \wedge Q)$
 2 sat asgmts #SAT, random sampling
 $(x > 5) \vee (x > 5 \wedge y < 10)$ ~~#SAT~~

③ What if the variables were quantified?

See M. Vardi's talk
 NP is the new P.

QBF

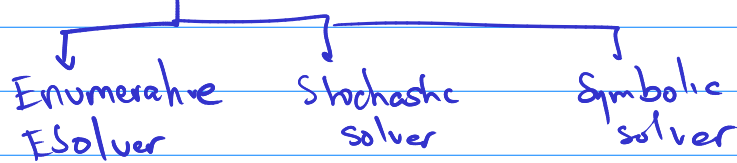
Unit 2: Program synthesis



$\forall x. \varphi(x)$ Syntax Guided Synthesis

$\varphi(x_1) \wedge \varphi(x_2)$

Counterexample Guided Inductive Synthesis (CEGIS)



① Synthesis from types $f: \text{List}\langle \text{Int} \rangle \rightarrow \text{Int}$

Type inhabitation, STLC ← simply typed lambda calculus

Curry-Howard correspondence Pspace complete

Types ↔ Propositions

Expressions ↔ Proofs

$x+5$

```

B  foo(A, B) (A a, A → B: f)
{
  return f(a);
}
    
```

$\forall A. B. A \rightarrow (A \rightarrow B) \rightarrow B$

$A \rightarrow (A \Rightarrow B) \Rightarrow B$

Unit 3: Proof techniques

Claim: Verifying loop-free code ^{over finite data domains} is easy.

Inductive invariants vs. (non-inductive) invariants.

Hoare logic

Resource usage analysis.

Assume $\log n$ program needs $O(n^2)$ time $an^2 + bn + c$

Safety properties / partial correctness

Liveness / termination checking

① Crash!

② Does not terminate

③ Exits successfully.

When we reach line 5, $x \neq \text{null}$.

Whenever we reach a line of code, some assertion always holds

We will eventually reach some line of code.

Think about fairness. COMPAS.

$f(x) \sim f(x+\delta)$ "Something is always true"

"Something will eventually be true".

Hyperproperties.

Logics of time — Amir Pnueli

Modeling the heap

Concurrency

```
int y=10;
int * x = &y;
```

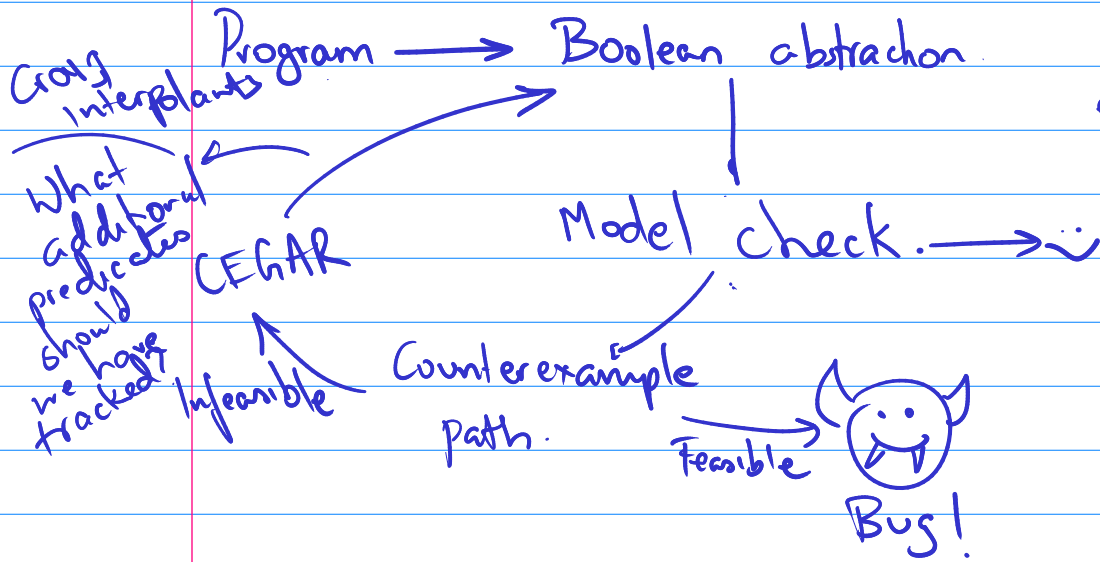
```
*x = 3;
```

```
int * x = malloc(sizeof(int));
```

Separation logic: Peter O'Hearn. → What is the value of y here?
Shape analysis
 $y = 3$.

Unit 4: Static analysis / predicate abstraction.

odd + odd = even
odd + even = odd
even + odd = odd
even + even = even.



② What research is happening today?

- Concurrency, fairness & privacy
 - `int x = 10;`
 - `int x ~ Unif(1, 10);`
- verification for AI \longleftrightarrow probabilistic programs
- AI for verification? \longleftrightarrow quantum programming languages
- Blockchains / smart contracts / distributed ledgers.
- Software defined networks
- How do we verify compilers themselves?

④ Big Picture

- Can we help programmers write better code?

Intent :

Verifying code Synthesis.

- Can we help programmers understand existing code?

Easier human-machine interfaces?